

# Mark Scheme (Results)

Summer 2013

GCE Core Mathematics 1 (6663/01)





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#### General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt[]{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.
- 8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

 $(x^2 + bx + c) = (x + p)(x + q)$ , where |pq| = |c|, leading to x =

 $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where |pq| = |c| and |mn| = |a|, leading to x =

## 2. <u>Formula</u>

Attempt to use <u>correct</u> formula (with values for *a*, *b* and *c*).

3. Completing the square

Solving 
$$x^2 + bx + c = 0$$
:  $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c$ ,  $q \neq 0$ , leading to  $x = ...$ 

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1.  $(x^n \rightarrow x^{n-1})$ 

2. Integration

Power of at least one term increased by 1.  $(x^n \rightarrow x^{n+1})$ 

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

# Answers without working

The rubric says that these  $\underline{may}$  not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

| Question<br>Number | Scheme  |  | Marks |
|--------------------|---|--|-------|
| 1                  | $\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(\sqrt{5}+1)}{(\sqrt{5}+1)}$  | Multiplies top and bottom by a correct expression. This statement is sufficient.   | M1    |
|                    | (Allow to multiply top and b  | ottom by $k(\sqrt{5}+1)$ )   |       |
|                    | $=\frac{\cdots}{4}$   | Obtains a denominator of 4 or<br>sight of $(\sqrt{5} - 1)(\sqrt{5} + 1) = 4$   | A1cso |
|                    | Note that M0A1 is not possible. The 4 mu  | ist come from a correct method.  |       |
|                    | $(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5}+5+7+\sqrt{5}$   | An attempt to multiply the<br>numerator by $(\pm\sqrt{5}\pm1)$ and<br>get 4 terms with at least 2<br>correct for their $(\pm\sqrt{5}\pm1)$ .<br>(May be implied)   | M1    |
|                    | $3 + 2\sqrt{5}$   | Answer as written or $a = 3$<br>and $b = 2$ . (Allow $2\sqrt{5} + 3$ )   | A1cso |
|                    | Correct answer with no work   | ing scores full marks  |       |
|                    |   |  | [4]   |
| Way 2              | $\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(-\sqrt{5}-1)}{(-\sqrt{5}-1)}$  | Statement is sufficient.   | M1    |
|                    | (Allow to multiply top and bottom by $k(-\sqrt{5}-1)$ )   |  |       |
|                    | $=\frac{\dots}{-4}$   | Obtains a denominator of -4  | A1cso |
|                    | $(7+\sqrt{5})(-\sqrt{5}-1) = -7\sqrt{5}-5-7-\sqrt{5}$   | An attempt to multiply the<br>numerator by $(\pm\sqrt{5}\pm 1)$ and<br>get 4 terms with at least 2<br>correct for their $(\pm\sqrt{5}\pm 1)$ .<br>(May be implied) | M1    |
|                    | $3+2\sqrt{5}$   | Answer as written or $a = 3$   | A1cso |
|                    | Connect on swort with no work   | and $b=2$  |       |
|                    | Correct answer with no work   |  | [4]   |
|                    | Alternative using Simulta   | neous Equations:   |       |
|                    | $\frac{(7+\sqrt{5})}{\sqrt{5}-1} = a + b\sqrt{5} \Rightarrow 7 + \sqrt{5} = (a-b)\sqrt{5} + 5b - a \text{ M1}$<br>Multiplies and collects rational and irrational parts<br>a-b=1, 5b-a=7  A1<br>Correct equations<br>a=3, b=2<br>M1 for attempt to solve simultaneous equations A1 both answers correct |  | 、     |

| Question<br>Number | Schen  | ıe  | Marks        |
|--------------------|--|---|--------------|
| 2                  | $(\int =)\frac{10x^5}{5} - \frac{4x^2}{2}, -\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$                      | M1: Some attempt to integrate:<br>$x^n \rightarrow x^{n+1}$ on at least one term.<br>(not for + c)<br>(If they think $\frac{3}{\sqrt{x}}$ is $3x^{\frac{1}{2}}$ you can<br>still award the method mark for<br>$\frac{1}{x^2} \rightarrow x^{\frac{3}{2}}$<br>A1: $\frac{10x^5}{5}$ and $\frac{-4x^2}{2}$ or better<br>A1: $-\frac{3x^{\frac{1}{2}}}{\frac{1}{2}}$ or better | M1A1, A1     |
|                    | $= \underline{2x^5 - 2x^2 - 6x^{\frac{1}{2}} + c}$<br>Do <b>not</b> apply isw. If they obtain the corr | Each term correct and simplified<br>and the + c all appearing together<br>on the same line. Allow $\sqrt{x}$ for<br>$x^{\frac{1}{2}}$ . Ignore any spurious integral<br>or signs and/or dy/dx's.  | A1           |
|                    | they lose the l  | ast mark.   | Г <i>А</i> Л |
|                    |  |   | [4]          |

| Question<br>Number | Scho  | eme  | Marks |
|--------------------|---|--|-------|
| 3(a)               | $8^{\frac{1}{3}} = 2$ or $8^5 = 32768$  | A correct attempt to deal with the $\frac{1}{3}$ or the 5.<br>$8^{\frac{1}{3}} = \sqrt[3]{8}$ or $8^{5} = 8 \times 8 \times 8 \times 8 \times 8$                 | M1    |
|                    | $\left(8^{\frac{5}{3}}\right) 32$   | Сао  | A1    |
|                    | A correct answer with no  | working scores full marks  |       |
|                    | Alterr  | native   |       |
|                    | $8^{\frac{5}{3}} = 8 \times 8^{\frac{2}{3}} = 8 \times 2^2 = N$<br>= 32   | 11 (Deals with the 1/3)<br>A1  |       |
|                    |   |  | (2)   |
| <b>(b)</b>         |   | One correct power either $2^3$ or $x^{\frac{3}{2}}$ .  |       |
|                    | $\left(2x^{\frac{1}{2}}\right)^3 = 2^3 x^{\frac{3}{2}}$   | $\left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) \text{ on its own}$<br>is not sufficient for this mark. | M1    |
|                    | $\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{-\frac{1}{2}} \text{ or } \frac{2}{\sqrt{x}}$  | M1: Divides coefficients of <i>x</i> and subtracts their powers of <i>x</i> . <b>Dependent on the previous M1</b>  | dM1A1 |
|                    |   | A1: Correct answer   |       |
|                    | Note that unless the power of x imp   | lies that they have subtracted their   |       |
|                    | powers you would need to see evidence of subtraction. E.g. $\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{\frac{1}{2}}$   |  |       |
|                    | would score dM0 unless you see some evidence that $3/2 - 2$ was intended for the power of <i>x</i> .  |  |       |
|                    | Note that there is a misconception that $\frac{\left(2x^{\frac{1}{2}}\right)^3}{4x^2} = \left(\frac{2x^{\frac{1}{2}}}{4x^2}\right)^3$ - this scores 0/3 |  |       |
|                    |   |  | (3)   |
|                    |   |  | [5]   |

| Question<br>Number | Sche   | eme   | Marks |
|--------------------|--|---|-------|
|                    | For this question, mark (a) and (  | b) together and ignore labelling.   |       |
| <b>4</b> (a)       | $(a_2 =) k(4+2) (= 6k)$  | Any correct (possibly un-simplified) expression   | B1    |
|                    |  |   | (1)   |
| (b)                | $a_3 = k$ (their $a_2 + 2$ ) (= $6k^2 + 2k$ )  | An attempt at $a_3$ . Can follow<br>through their answer to (a) but $a_2$<br>must be an expression in k.                                    | M1    |
|                    | $a_1 + a_2 + a_3 = 4 + (6k) + (6k^2 + 2k)$   | An attempt to find their $a_1 + a_2 + a_3$  | M1    |
|                    | $4 + (6k) + (6k^2 + 2k) = 2$   | A correct equation in any form.   | A1    |
|                    | Solves $6k^2 + 8k + 2 = 0$ to obtain $k = (6k^2 + 8k + 2 = 2(3k + 1)(k + 1))$  | Solves their 3TQ as far as $k =$<br>according to the general principles.<br>(An independent mark for solving<br>their three term quadratic) | M1    |
|                    | k = -1/3   | Any equivalent fraction   | A1    |
|                    | <i>k</i> = – 1   | Must be from a correct equation.<br>(Do not accept un-simplified)   | B1    |
|                    | Note that it is quite common to think the sequence is an AP. Unless they find $a_3$ , this is likely only to score the M1 for solving their quadratic. |   |       |
|                    |  |   | (6)   |
|                    |  |   | [7]   |

| Question<br>Number | Sche  | eme  | Marks  | 5   |
|--------------------|---|--|--------|-----|
| 5 (a)              | 6x + x > 1 - 8                                    | Attempts to expand the bracket and collect <i>x</i> terms on one side and constant terms on the other.<br>Condone sign errors and allow one error in expanding the bracket.<br>Allow $\leq, \leq, \geq$ ,= instead of >.   | M1     |     |
|                    | x > -1  | Cao  | A1     |     |
|                    | Do not isw here, mar                              | k their final answer.  |        |     |
|                    |   |  |        | (2) |
| (b)                | (x+3)(3x-1)[=0]                                   | M1: Attempt to solve the quadratic to obtain two critical values   |        |     |
|                    | $\Rightarrow x = -3 \text{ and } \frac{1}{3}$     | A1: $x = -3$ and $\frac{1}{3}$ (may be implied by their inequality). Allow all equivalent fractions for -3 and 1/3. (Allow 0.333)  | M1A1   |     |
|                    |   | for 1/3)   |        |     |
|                    | $-3 < x < \frac{1}{3}$                            | M1: Chooses "inside" region (The<br>letter x does not need to be used<br>here)<br>A1ft: Allow $x < \frac{1}{3}$ and $x > -3$ or<br>$\left(-3, \frac{1}{3}\right)$ or $x < \frac{1}{3} \cap x > -3$ . Follow<br>through their critical values. (must<br>be in terms of x here) Allow all<br>equivalent fractions for -3 and 1/3.<br>Both ( $x < \frac{1}{3}$ or $x > -3$ ) and<br>( $x < \frac{1}{3}$ , $x > -3$ ) as a final answer<br>score A0. | M1A1ft |     |
|                    |   |  |        | (4) |
|                    |   | •  |        | [6] |
|                    | Note that use of $\leq$ or $\geq$ appearing in an | otherwise correct answer in (a) or (b)   |        |     |
|                    | should only be penalised or                       | nce, the first time it occurs.   |        |     |

| Question<br>Number | Scheme  |   | Marks |
|--------------------|---|---|-------|
| 6                  | (-1, 3) ,   | (11, 12)  |       |
| (a)                | $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{12 - 3}{11 - (-1)}, = \frac{3}{4}$   | M1:Correct method for the gradient<br>A1: Any correct fraction or<br>decimal                        | M1,A1 |
|                    | $y-3 = \frac{3}{4} (x+1) \text{ or } y - 12 = \frac{3}{4} (x-11)$<br>or $y = \frac{3}{4} x + c \text{ with attempt at}$<br>substitution to find c | Correct straight line method using<br>either of the given points and a<br>numerical gradient.       | M1    |
|                    | 4y - 3x - 15 = 0  | Or equivalent with integer<br>coefficients (= 0 <b>is</b> required)                                 | A1    |
|                    | This A1 should only   | be awarded in (a)   |       |
|                    |   |   | (4)   |
| (a)<br>Way 2       | $\frac{y - y_1}{y_1 - y_1} = \frac{x - x_1}{x_1 - x_1} \Longrightarrow \frac{y - 3}{12 - 3} = \frac{x + 1}{11 + 1}$                               | M1: Use of a correct formula for the straight line  | M1A1  |
| way 2              | $y_2 - y_1$ $x_2 - x_1$ $12 - 3$ $11 + 1$   | A1: Correct equation  |       |
|                    | 12(y-3) = 9(x+1)  | Eliminates fractions  | M1    |
|                    | 4y - 3x - 15 = 0  | Or equivalent with integer<br>coefficients (= 0 <b>is</b> required)                                 | A1    |
|                    |   |   | (4)   |
| (b)                | Solves their equation from part (a) and $L_2$ simultaneously to eliminate one variable  | Must reach as far as an equation in <i>x</i> only or in <i>y</i> only. (Allow slips in the algebra) | M1    |
|                    | x = 3 or $y = 6$  | One of $x = 3$ or $y = 6$   | A1    |
|                    | <b>Both</b> $x = 3$ and $y = 6$   | Values can be un-simplified fractions.  | A1    |
|                    | Fully correct answers with no   | working can score 3/3 in (b)  |       |
|                    |   |   | (3)   |
|                    |   |   |       |
| (b)<br>Way 2       | $(-1,3) \rightarrow -a + 3b + c = 0$<br>$(11,12) \rightarrow 11a + 12b + c = 0$   | Substitutes the coordinates to obtain two equations   | M1    |
|                    | $\therefore a = -\frac{3}{4}b, \ b = -\frac{4}{15}c$  | Obtains sufficient equations to establish values for <i>a</i> , <i>b</i> and <i>c</i>               | A1    |
|                    | e.g. $c = 1 \Longrightarrow b = -\frac{4}{15}, a = \frac{3}{15}$  | Obtains values for <i>a</i> , <i>b</i> and <i>c</i>   | M1    |
|                    | $\frac{3}{15}x - \frac{4}{15}y + 1 = 0 \Longrightarrow 4y - 3x - 15 = 0$  | Correct equation  | A1    |
|                    |   |   | (4)   |
|                    |   |   | [7]   |

| Question<br>Number | Scheme   | e  | Marks  |
|--------------------|--|--|--------|
| 7(a)               | $600 = 200 + (N-1)20 \Longrightarrow N = \dots$  | Use of 600 with a <u>correct</u><br>formula in an attempt to find <i>N</i> .<br>A correct formula could be<br>implied by a correct answer.   | M1     |
|                    | N = 21   | cso  | A1     |
|                    | Accept correct an  | swer only.   |        |
|                    | $600 = 200 + 20N \implies N = 20$ is<br>$\frac{600 - 200}{20} = 20 \therefore N = 21$ is M1A                           | M0A0 (wrong formula)<br>1 (correct formula implied)  |        |
|                    | Listing: All terms must be listed up to  | 600 and 21 correctly identified.   |        |
|                    | A solution that scores 2 if fully  | correct and 0 otherwise.   | (-)    |
|                    |  |  | (2)    |
| (b)                | Look for an A  | AP first:  |        |
|                    | $S = \frac{21}{2}(2 \times 200 + 20 \times 20) \text{ or } \frac{21}{2}(200 + 600)$                                    | M1: Use of correct sum formula<br>with their <b>integer</b> $n = N$ or $N - 1$<br>from part (a) where $3 < N < 52$   |        |
|                    | $S = \frac{20}{2} (2 \times 200 + 19 \times 20) \text{ or } \frac{20}{2} (200 + 580)$                                  | and $a = 200$ and $d = 20$ .<br>A1: Any correct un-simplified  | M1A1   |
|                    | (= 8400 or 7800)   | numerical expression with $n = 20$<br>or $n = 21$ (No follow through<br>here)  |        |
|                    | Then for the cons  | tant terms:  |        |
|                    | $600 \times (52 - "N") (= 18600)$  | M1: $600 \times k$ where k is an<br>integer and $3 \le k \le 52$<br>A1: A correct un-simplified<br>follow through expression with<br>their k consistent with n so that<br>n + k = 52 | M1A1ft |
|                    | So total is 27000  | Cao  | A1     |
|                    | Note that for the constant terms, they may   | correctly use an AP sum with $d = 0$ .   |        |
|                    | There are no marks in (b)  | ) for just finding S <sub>52</sub>   |        |
|                    |  |  | (5)    |
|                    |  |  | [7]    |
|                    | If they obtain $N = 20$ in (a) (0/2) and<br>$S = \frac{20}{2}(2 \times 200 + 19 \times 20) + 32 \times 600$            | nd then in (b) proceed with,<br>0 = 7800 + 19 200 = 27 000   |        |
|                    | allow them to 'recover' and score full marks in (b)  |  |        |
|                    | Similarl<br>If they obtain $N = 22$ in (a) (0/2) an<br>$S = \frac{21}{2}(2 \times 200 + 20 \times 20) + 31 \times 600$ | y<br>nd then in (b) proceed with,<br>0 = 8400 + 18 600 = 27 000  |        |
|                    | allow them to 'recover' and score full marks in (b)  |  |        |

| Question<br>Number | Schem  | e   | Marks |     |
|--------------------|--|---|-------|-----|
| 8                  |  | Horizontal translation – does <b>not</b><br>have to cross the <i>y</i> -axis on the right<br>but must at least reach the <i>x</i> -axis.  | B1    |     |
| (a)                |  | Touching at $(-5, 0)$ . This could be<br>stated anywhere or $-5$ could be<br>marked on the <i>x</i> -axis. Or $(0, -5)$<br><b>marked in the correct place.</b> Be<br>fairly generous with 'touching' if<br>the intention is clear.  | B1    |     |
| (a)                | ν  | The right hand tail of their cubic<br>shape crossing at $(-1, 0)$ . This<br>could be stated anywhere or $-1$<br>could be marked on the <i>x</i> -axis. Or<br>(0, -1) <b>marked in the correct</b><br><b>place.</b> The curve must <b>cross</b> the<br><i>x</i> -axis and not stop at $-1$ . | B1    |     |
|                    |  |   | (     | (3) |
| (b)                | $(x+5)^2(x+1)$                               | Allow $(x+3+2)^2(x-1+2)$  | B1    |     |
|                    |  |   | (     | (1) |
| (c)                | When $x = 0, y = 25$                         | M1: Substitutes $x = 0$ into their<br>expression in <b>part</b> ( <b>b</b> ) which is<br>not $f(x)$ . This may be implied by<br>their answer.<br>Note that the question asks them<br>to use part (b) but allow<br>independent methods.<br>A1: $y = 25$ (Coordinates not<br>needed)          | M1 A1 |     |
|                    | If they expand <u>incorrectly</u> prior to s | ubstituting $x = 0$ , score M1 A0   |       |     |
|                    | <b>NB</b> $f(x + 2) = x^3 + 1$               | $1x^2 + 35x + 25$   |       |     |
|                    |  |   | (     | (2) |
|                    |  |   |       | 6   |

| Question<br>Number |  | Scheme  | Marks   |
|--------------------|--|---|---------|
| 9 (a)              | $(3-x^2)^2 = 9 - 6x^2 + x^4$   | An attempt to expand the numerator<br>obtaining an expression of the form<br>$9 \pm px^2 \pm qx^4$ , $p, q \neq 0$  | M1      |
|                    | $9x^{-2} + x^2$  | Must come from $\frac{9+x^4}{x^2}$  | A1      |
|                    | -6   | Must come from $\frac{-6x^2}{x^2}$  | A1      |
|                    | Alternative 1: Writes $\frac{(3-x^2)^2}{x^2}$ as $(3x^{-1}-x)^2$ and attempts to expand = M1 |   |         |
|                    |  |   |         |
|                    | Alternative 2: Sets $(3 - x^2)^2 = 9 + x^2$<br>coefficients = M1 t                           | $Ax^2 + Bx^4$ , expands $(3 - x^2)^2$ and compares<br>hen A1A1 as in the scheme.  |         |
|                    |  |   | (3)     |
|                    | (f'(x)   | $=9x^{-2}-6+x^2)$   |         |
| (b)                | $-18x^{-3} + 2x$   | M1: $x^n \rightarrow x^{n-1}$ on separate terms at least<br>once. Do not award for $A \rightarrow 0$<br>(Integrating is M0)   | M1 A1ft |
|                    |  | Alft: $-18x^3 + 2^{n}B^{n}x$ with a numerical <i>B</i><br>and no extra terms. (A may have been<br>incorrect or even zero)   |         |
|                    |  | n n⊥1   | (2)     |
|                    |  | M1: $x^n \rightarrow x^{n+1}$ on separate terms at least once. (Differentiating is M0)  |         |
| (c)                | $f(x) = -9x^{-1} - 6x + \frac{x^3}{3}(+c)$   | A1ft: $-9x^{-1} + Ax + \frac{Bx^3}{3}(+c)$ with   | M1A1ft  |
|                    |  | numerical A and B, $A, B \neq 0$  |         |
|                    | $10 = \frac{-9}{-3} - 6(-3) + \frac{(-3)^3}{3} + c \text{ so } c$ $= \dots$                  | Uses $x = -3$ and $y = 10$ in what they think<br>is $f(x)$ (They may have differentiated<br>here) but it must be a changed function<br>i.e. not the original $f'(x)$ , to form a linear<br>equation in <i>c</i> and attempts to find <i>c</i> . No<br>+ <i>c</i> gets M0 and A0 unless their method<br>implies that they are correctly finding a<br>constant. | M1      |
|                    | <i>c</i> = -2  | cso   | A1      |
|                    | $(f(x) =) -9x^{-1} - 6x + \frac{x^3}{3} + \text{their}$<br>c                                 | Follow through their <i>c</i> in an otherwise<br>(possibly un-simplified) <b>correct</b><br><b>expression</b> .<br>Allow $-\frac{9}{x}$ for $-9x^{-1}$ or even $\frac{9x^{-1}}{-1}$ .   | A1ft    |
|                    | Note that if they integrate in (b),  | no marks there but if they then go on to  |         |
|                    | use their integration in (c), th   | e marks for integration are available.  | (5)     |
|                    |  |   | [10]    |
| L                  |  | 1   |         |

| Question<br>Number      | Scheme  | Marks   |       |            |
|-------------------------|---|---|-------|------------|
| 10(a)                   | $x^2 - 4k(1 - 2x) + 5k(=0)$   | Makes <i>y</i> the subject from the first equation<br>and substitutes into the second equation<br>(= 0 not needed here) or eliminates <i>y</i> by a<br>correct method.  | M1    |            |
|                         | So $x^2 + 8kx + k = 0 *$  | Correct completion to printed answer. There must be no incorrect statements.  | Alcso |            |
| (b)                     | $\left(8k\right)^2 - 4k$  | M1: <u>Use</u> of $b^2 - 4ac$ (Could be in the<br>quadratic formula or an inequality, = 0 not<br>needed yet). There must be some correct<br>substitution but there must be no x's. No<br>formula quoted followed by e.g.<br>$8k^2 - 4k = 0$ is M0.<br>A1: Correct expression. Do not condone<br>missing brackets unless they are implied by<br>later work but can be implied by $(8k)^2 > 4k$<br>etc. | M1 A1 | (2)        |
|                         | $k = \frac{1}{16} \text{ (oe)}$   | Cso (Ignore any reference to $k = 0$ ) but there<br>must be no contradictory earlier statements.<br>A fully correct solution with no errors.  | A1    | (2)        |
| (b)                     |   | M1: Correct strategy for equal roots  |       | (3)        |
| Way 2<br>Equal<br>roots | $\Rightarrow x^{2} + 8kx + k = (x + \sqrt{k})^{2}$ $\Rightarrow 8k = 2\sqrt{k}$                 | A1: Correct equation  | M1A1  |            |
|                         | $k = \frac{1}{16} \text{ (oe)}$   | Cso (Ignore any reference to $k = 0$ )  | A1    |            |
|                         | Completes the Square<br>$r^{2} + 8kx + k = (x + 4k)^{2} - 16k^{2} + k$                          | M1: $(x \pm 4k)^2 \pm p \pm k, \ p \neq 0$  |       |            |
| (b)<br>Way 3            | $\Rightarrow 16k^2 - k = 0$   | A1: Correct equation  | M1A1  |            |
|                         | $k = \frac{1}{16} \text{ (oe)}$   | Cso (Ignore any reference to $k = 0$ )  | A1    |            |
|                         |   |   |       | (3)        |
| (c)                     | $x^{2} + \frac{1}{2}x + \frac{1}{16} = 0$ so<br>$(x + \frac{1}{4})^{2} = 0 \Longrightarrow x =$ | Substitutes their value of $k$ into the given<br>quadratic and attempt to solve their 2 or 3<br>term quadratic as far as $x =$ (may be implied<br>by substitution into the quadratic formula) or<br>starts again and substitutes their value of $k$<br>into the second equation and solves<br>simultaneously to obtain a value for $x$ .  | M1    |            |
|                         | $x = -\frac{1}{4}, y = 1\frac{1}{2}$  | First A1 one answer correct, second A1 both answers correct.  | A1A1  |            |
|                         | <b>Special Case:</b> $x^2 + \frac{1}{2}x + \frac{1}{16} = 0 \Rightarrow$                        | $x = -\frac{1}{4}, \ \frac{1}{4} \Rightarrow y = 1\frac{1}{2}, \ \frac{1}{2}$ allow M1A1A0  |       |            |
|                         |   |   |       | (3)<br>[9] |
|                         |   |   | 1     | ႞ႄ႞        |

| Question<br>Number | Scheme   |   | Marks    |
|--------------------|--|---|----------|
| 11<br>(a)          | $\left(-\frac{3}{4}, 0\right).  \text{Accept}  x = -\frac{3}{4}$                 |   | B1       |
|                    |  |   | (1)      |
| <b>(b)</b>         | y = 4  | B1: One correct asymptote   |          |
|                    | x = 0 or 'y-axis'  | B1: Both correct asymptotes and no extra ones.  | B1B1     |
|                    | Special case $x \neq 0$ and  | <b>d</b> $y \neq 4$ scores B1B0   |          |
|                    |  |   | (2)      |
| (c)                | $\frac{\mathrm{d}y}{\mathrm{d}x} = -3x^{-2}$                                     | $\frac{\mathrm{d}y}{\mathrm{d}x} = kx^{-2} (\text{Allow } \frac{\mathrm{d}y}{\mathrm{d}x} = kx^{-2} + 4)$   | M1       |
|                    | At $x = -3$ , gradient of curve $= -\frac{1}{3}$                                 | Cao (may be un-simplified but must<br>be a fraction with no powers) e.g.<br>$-3(-3)^{-2}$ scores A0 unless evaluated<br>as e.g. $\frac{-3}{9}$ or is implied by their<br>normal gradient.   | A1       |
|                    | Gradient of normal = $-1/m$  | Correct perpendicular gradient rule<br>applied to a numerical gradient that<br>must have come from substituting <i>x</i><br>= -3 into their derivative.<br><b>Dependent on the previous M1.</b>   | dM1      |
|                    | Normal at <i>P</i> is $(y-3) = 3(x+3)$   | M1: Correct straight line method<br>using (-3, 3) and a "changed"<br>gradient. A wrong equation with no<br>formula quoted is M0. <b>Also</b><br><b>dependent on the first M1.</b><br>A1: Any correct equation   | dM1A1    |
|                    |  |   | (5)      |
| ( <b>d</b> )       | (-4, 0) and (0, 12).   | Both correct<br>(May be seen on a sketch)   | B1       |
|                    | So <i>AB</i> has length $\sqrt{160}$<br>or <i>AB</i> <sup>2</sup> has length 160 | M1: Correct use of Pythagoras for<br>their <i>A</i> and <i>B</i> one of which lies on<br>the <i>x</i> -axis and the other on the<br><i>y</i> -axis, obtained from their<br>equation in (c). A correct method<br>for $AB^2$ or $AB$ .<br>A1: $\sqrt{160}$ or better e.g. $4\sqrt{10}$ with<br>no errors seen | M1 A1cso |
|                    |  |   | (3)      |
|                    |  |   | [11]     |

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